

# IMMEDIATE DEFLECTION OF STRUCTURAL CONCRETE MEMBERS

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## **Abstract**

This report addresses the deflection of structural concrete members of concrete structures. It outlines why deflection is important, its major influence on the final extent of cracking and the magnitude of deflection in structures, and what to do about it in design. A model is presented for predicting the deflection strain in normal and high strength concrete and the time-dependent behavior of plain concrete and reinforced concrete, with and without external restraints, is explained. Analytical procedures are described for estimating the final width and spacing of both flexural cracks and direct tension cracks and a simplified procedure is presented for including the effects of shrinkage when calculating long-term deflection.

## **1.0 Introduction**

For a concrete structure to be serviceable, cracking must be controlled, and deflections must not be excessive. It must also not vibrate excessively. Concrete shrinkage plays a major role in each of these aspects of the service load behavior of concrete structures. The design for serviceability is possibly the most difficult and least well understood aspect of the design of

concrete structures. Service load behavior depends primarily on the properties of the concrete, and these are often not known reliably at the design stage. Moreover, concrete behaves in a non-linear and inelastic manner at service loads. The non-linear behavior that complicates serviceability calculations is due to cracking, tension stiffening, creep, and shrinkage [1]. Of these, shrinkage is the most problematic. Restraint to shrinkage causes time-dependent cracking and gradually reduces the beneficial effects of tension stiffening. It results in a gradual widening of existing cracks and, in flexural members, a significant increase in deflections with time. The control of cracking in a reinforced or prestressed concrete structure is usually achieved by limiting the stress increment in the bonded reinforcement to some appropriately low value and ensuring that the bonded reinforcement is suitably distributed. Many codes of practice specify maximum steel stress increments after cracking and maximum spacing requirements for the bonded reinforcement. However, few existing code procedures, if any, account adequately for the gradual increase in existing crack widths with time, due primarily to shrinkage, or the time-dependent development of new cracks resulting from tensile stresses caused by restraint to shrinkage. For deflection control, the structural designer should select maximum deflection limits that are appropriate to the structure and its intended use. The calculated deflection (or camber) must not exceed these limits. Codes of practice give general guidance for both the selection of the maximum deflection limits and the calculation of deflection. However, the simplified procedures for calculating deflection in most codes were developed from tests on simply supported reinforced concrete beams and often produce grossly inaccurate predictions when applied to more complex structures. Again, the existing code procedures do not provide real guidance on how to adequately model the time-dependent effects of creep and shrinkage in deflection calculations. Serviceability failures of concrete structures involving excessive cracking and/or excessive deflection are relatively common. Numerous cases have been reported, in Australia and elsewhere, of structures that complied with code requirements but still deflected or cracked excessively. In a large majority of these failures, shrinkage of concrete is primarily responsible [2]. Clearly, the serviceability provisions embodied in our code do not adequately model the in-service behavior of structures and fail to account adequately for shrinkage. The quest for serviceable concrete structures must involve the development of more reliable design procedures. It must also involve designers giving more attention to the specification of an appropriate concrete mix, particularly about the creep and shrinkage characteristics of the mix, and sound engineering input is required in the construction procedures. High performance concrete structures require the specification of high-performance concrete (not necessarily high strength concrete, but concrete with relatively

low shrinkage, not prone to plastic shrinkage cracking) and a high standard of construction, involving suitably long stripping times, adequate propping, effective curing procedures and rigorous on-site supervision [3].

## 2. Designing for Serviceability

When designing for serviceability, the designer must ensure that the structure can perform its intended function under the day-to-day service loads. Deflection must not be excessive; cracks must be adequately controlled, and no portion of the structure should suffer excessive vibration. Shrinkage causes time-dependent cracking, thereby reducing the stiffness of a concrete structure, and is therefore a detrimental factor in all aspects of the design for serviceability. Deflection problems that may affect the serviceability of concrete structures can be classified into three main types:

- (a) Where excessive deflection causes either aesthetic or functional problems.
- (b) Where excessive deflection results in damage to either structural or non-structural element attached to the member.
- (c) Where dynamics effects due to insufficient stiffness cause discomfort to occupants.

Examples of deflection problems of type (a) include objectionable visual sagging (or hogging), and ponding of water on roofs. In fact, any deflection that prevents a member fulfilling its intended function causes a problem of this type. Type (a) problems are generally overcome by limiting the total deflection to some appropriately low value. The total deflection is the sum of the short-term and time-dependent deflection caused by the dead load (including self-weight), the prestress (if any), the expected in-service live load, and the load-independent effects of shrinkage and temperature changes. When the total deflection exceeds about  $\text{span}/200$  below the horizontal, it may become visually unacceptable. The designer must decide on the maximum limiting value for the total deflection and this limit must be appropriate for the member and its intended function [4]. A total deflection limit of  $\text{span}/200$ , for example, may be appropriate for the floor of a car park, but is inadequate for gymnasium floor which may be required to remain essentially plane under service conditions. Examples of type (b) problems include deflections resulting in cracking of masonry walls or other partitions, damage to ceiling or floor finishes, and improper functioning of sliding windows and doors. To avoid these problems, a limit must be placed on that part of the total deflection that occurs after the attachment of such elements [5]. This incremental deflection is usually the sum of the long-

term deflection due to all the sustained loads and shrinkage, the short-term deflection due to the transitory live load, and any temperature-induced deflection. AS 3600 (1994) [3] limits the incremental deflection for members supporting masonry partitions to between span/500 and span/1000, depending on the provisions made to minimize the effect of movement.

Type (c) deflection problems include the perceptible springy vertical motion of floor systems and other vibration-related problems. Very little quantitative information for controlling vibration is available in codes of practice. ACI 318-99 [5] places a limit of span/360 on the short-term deflection of a floor due to live load. This limit provides a minimum requirement on the stiffness of members that may, in some cases, be sufficient to avoid problems of type (c).

Excessively wide cracks can be unsightly and spoil the appearance of an exposed concrete surface; they can allow the ingress of moisture accelerating corrosion of the reinforcement and durability failure; and, in exceptional cases, they can reduce the contribution of the concrete to the shear strength of a member. Excessively wide cracks in floor systems and walls may often be avoided by the inclusion of strategically placed contraction joints, thereby removing some of the restraint to shrinkage and reducing the internal tension [6]. When cracking does occur, to ensure that crack widths remain acceptably small, adequate quantities of well distributed and well-anchored reinforcement must be included at every location where significant tension will exist.

The maximum crack width that may be acceptable in each situation depends on the type of structure, the environment, and the consequences of excessive cracking. In corrosive and aggressive environments, crack widths should not exceed 0.1 - 0.2 mm [7]. For members with one or more exposed surfaces, a maximum crack width of 0.3 mm should provide visual acceptability. For the sheltered interior of most buildings where the concrete is not exposed and aesthetic requirements are of secondary importance, larger crack widths may be acceptable (say 0.5 mm or larger) [8].

### **3.0 Effects of Shrinkage**

If concrete members were free to shrink, without restraint, shrinkage of concrete would not be a major concern to structural engineers. However, this is not the case. The contraction of a concrete member is often restrained by its supports or by the adjacent structure. Bonded reinforcement also restrains shrinkage. Each of these forms of restraint involve the imposition of a gradually increasing tensile force on the concrete which may lead to time-dependent

cracking (in previously uncracked regions), increases in deflection and a widening of existing cracks. Restraint to shrinkage is probably the most common cause of unsightly cracking in concrete structures. In many cases, these problems arise because shrinkage has not been adequately considered by the structural designer and the effects of shrinkage are not adequately modelled in the design procedures specified in codes of practice for crack control and deflection calculation [9].

The advent of shrinkage cracking depends on the degree of restraint to shrinkage, the extensibility and strength of the concrete in tension, tensile creep and the load induced tension existing in the member. Cracking can only be avoided if the gradually increasing tensile stress induced by shrinkage, and reduced by creep, is always less than the tensile strength of the concrete. Although the tensile strength of concrete increases with time, so too does the elastic modulus and, therefore, so too does the tensile stress induced by shrinkage [10]. Furthermore, the relief offered by creep decreases with age.

The existence of load induced tension in uncracked regions accelerates the formation of time dependent cracking. In many cases, therefore, shrinkage cracking is inevitable. The control of such cracking requires two important steps. First, the shrinkage-induced tension and the regions where shrinkage cracks are likely to develop must be recognised by the structural designer [11].

Second, an adequate quantity and distribution of anchored reinforcement must be included in these regions to ensure that the cracks remain fine, and the structure remains serviceable.

## 4.0 The process of Deflections in RC members

Reinforced concrete is used in modern construction as a reliable and affordable material for suspended flooring. Reinforced concrete slabs and beams are considerably durable, however, they deflect over time. A crucial part of the structural design of reinforced concrete elements is to prevent deflections from reaching intolerable levels known as deflection limits. In addition to being unsightly, excessive deflection can make building occupants uncomfortable and can cause cracks to non-structural elements such as partitions as these elements won't likely be flexible enough unless they are articulated.

Although reinforced concrete is a durable material and is considered suitable for aggressive environmental conditions it still has some disadvantages such as the propensity for cracking

due to flexure, drying shrinkage, and thermal effects, as well as deflections brought on by shrinkage and creep. There are types of Deflections:

#### 4.1 INSTANTANEOUS DEFLECTION

The deflection of structural members is due mainly to the dead load plus a fraction of or all the live loads. The deflection that occurs immediately upon applying the load is called the immediate, or instantaneous deflection.

#### 4.2 LONG-TIME DEFLECTION

The deflection of reinforced concrete members continues to increase under sustained load, although more slowly with time. Shrinkage and creep are the cause of this additional deflection, which is called long-time deflection [3].

### 5.0 Instantaneous (Immediate) Deflection

Under sustained loads, the deflection increases appreciably with time. Various methods are available for computing deflections in statically determinate and indeterminate structures. The instantaneous deflection calculations are based on the elastic behavior of the flexural members. The elastic deflection,  $\Delta$ , is a function of the load,  $W$ , span,  $L$ , moment of inertia,  $I$ , and modulus of elasticity of the material,  $E$ :

$$\Delta = \frac{5WL^3}{384EI} = \frac{5wL^4}{384EI}$$

Where:

$W = wL$  (uniform load per unit length  $\times$  span) is the total load on the span. Deflections of beams with different loadings and different end conditions as a function of the load, span, and  $EI$  are given in Appendix C in books of structural analysis. Because  $W$  and  $L$  are known, the problem is to calculate the modulus of elasticity,  $E$ , and the moment of inertia,  $I$ , of the concrete member or the flexural stiffness of the member,  $EI$ .

#### 5.1 Moment of Inertia

It's important to remember that the moment of inertia changes with load, making our deflection equations non-linear concerning loading. We can't use superposition to determine load combinations because the moment of inertia is different for each load case, and the parts are no longer additive. This means we can't simply add the deflection due to dead load and live

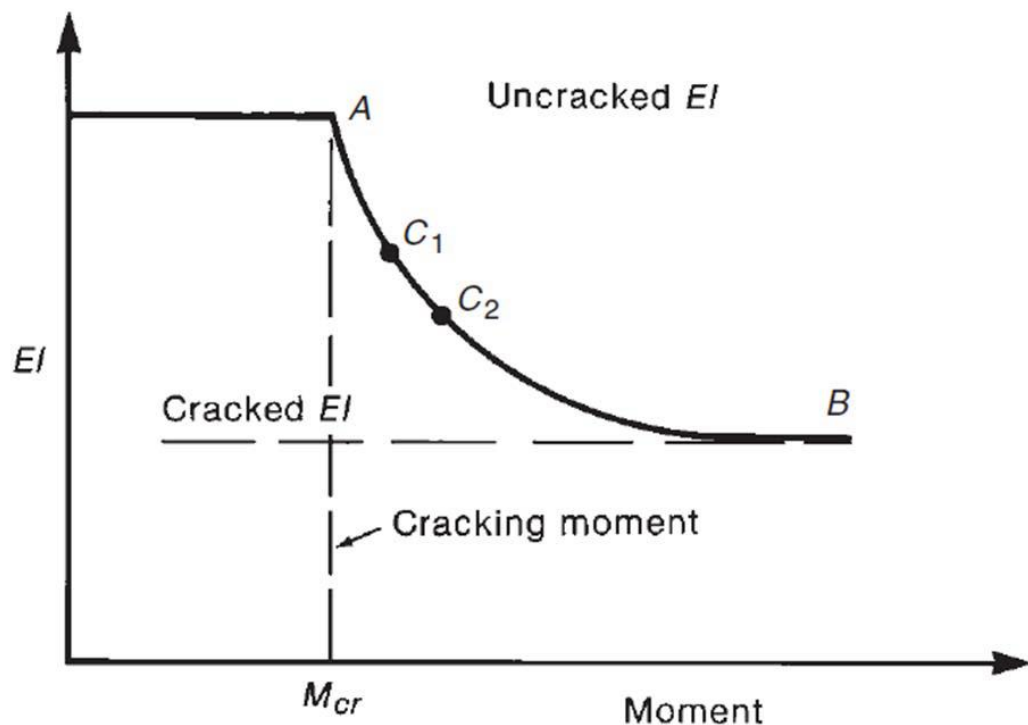
load to find the total load deflection, as we can in other materials where both deflection calculations use the same moment of inertia.

### 5.1.1 Calculating the moment of inertia.

The most common method for computing the section properties of a composite section is known as the transformed section method. This involves transforming the steel to an equivalent area of concrete by multiplying the area of each bar set by the modular ratio ( $n = E_s/E_c$ ). This transformed area allows us to use normal statics equations to determine the location of the elastic neutral axis and the axis-dependent properties such as the moment of inertia of the transformed section.

### 5.1.2 Uncracked Section

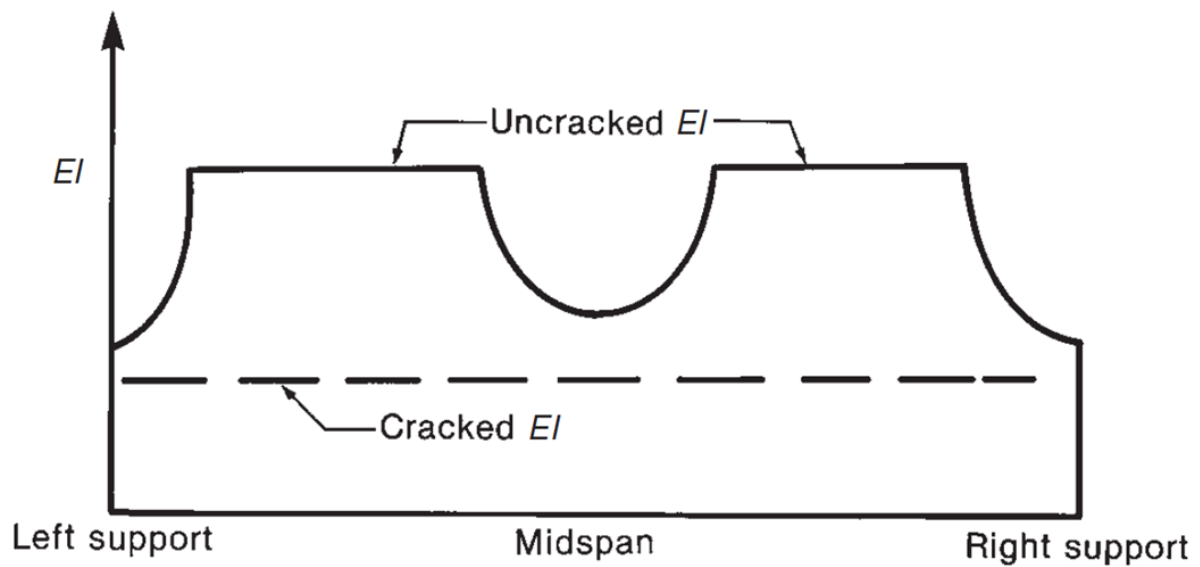
In most reinforced concrete beams, the moment of inertia for an uncracked section based on a transformed area is like the moment of inertia of the gross section without transforming the



(e) Variation in EI with moment.

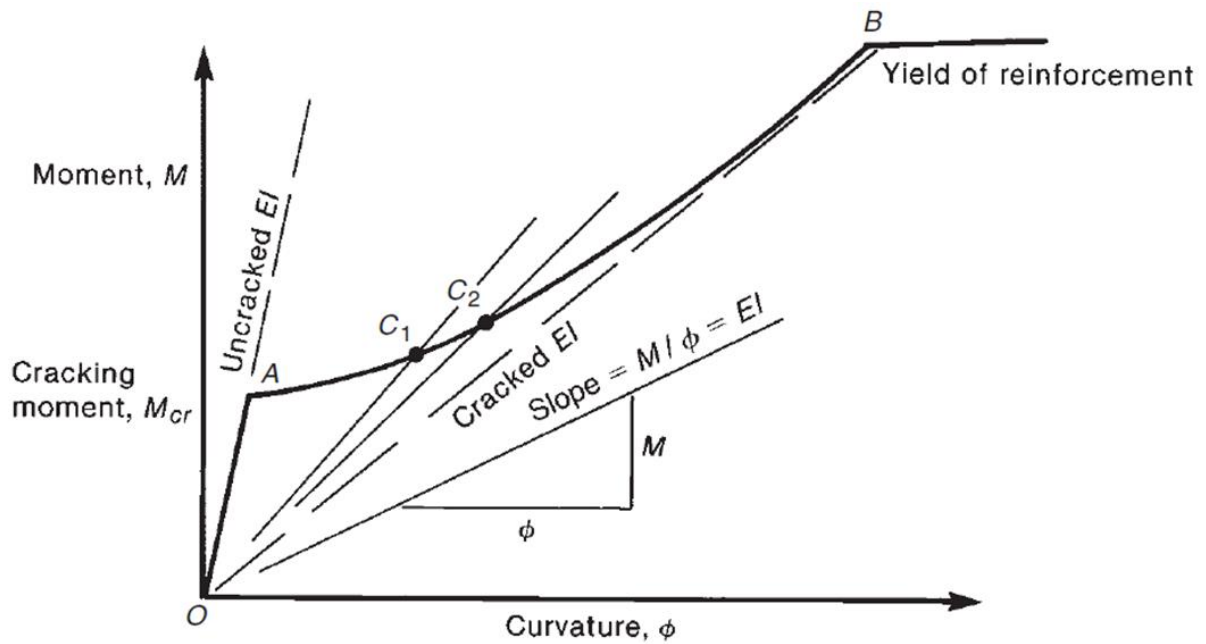
steel. This is because the steel is a small portion of the overall cross-section. Therefore, it's appropriate to use the moment of inertia without transforming the section when cracking is not present, as the untransformed section's moment of inertia is conservative.





### 5.1.3 Cracking Moment

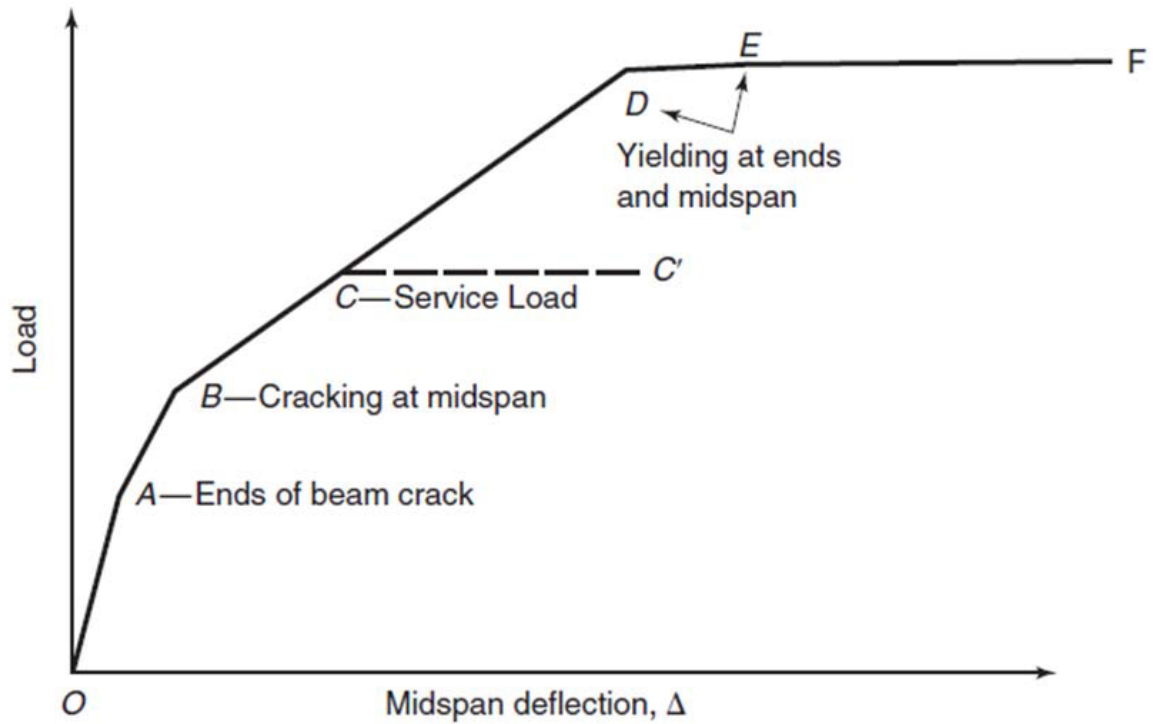
Cracks occur when the tensile bending stress in the concrete exceeds the concrete's ability to resist it. To predict cracking, you can determine the moment that causes cracking to occur and compare it to the actual moments. The cracking moment ( $M_{cr}$ ) is found by setting the elastic flexural stress equation ( $Mc/I$ ) equal to the tensile stress capacity of the concrete ( $f_r$ , also known as the modulus of rupture) and then solving for  $M$ . The equation can be found in ACI 318 9.5.2.3.



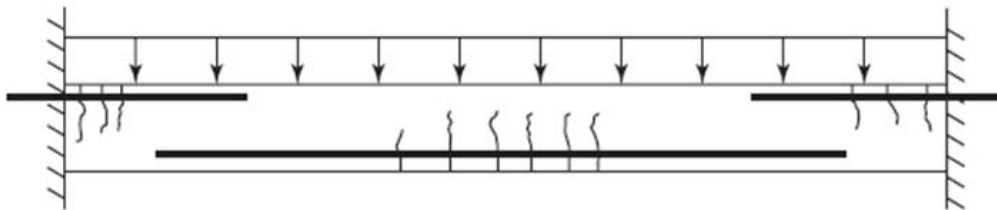
(d) Moment-curvature diagram.

### 5.1.3 Midspan Deflection:

Midspan deflections refer to the vertical displacements occurring at the midpoint of a beam or structural element due to applied loads. These deflections are critical in structural engineering as they affect the overall performance, safety, and serviceability of structures. Here's a detailed overview of midspan deflections, including their significance, calculation methods, and factors influencing them.

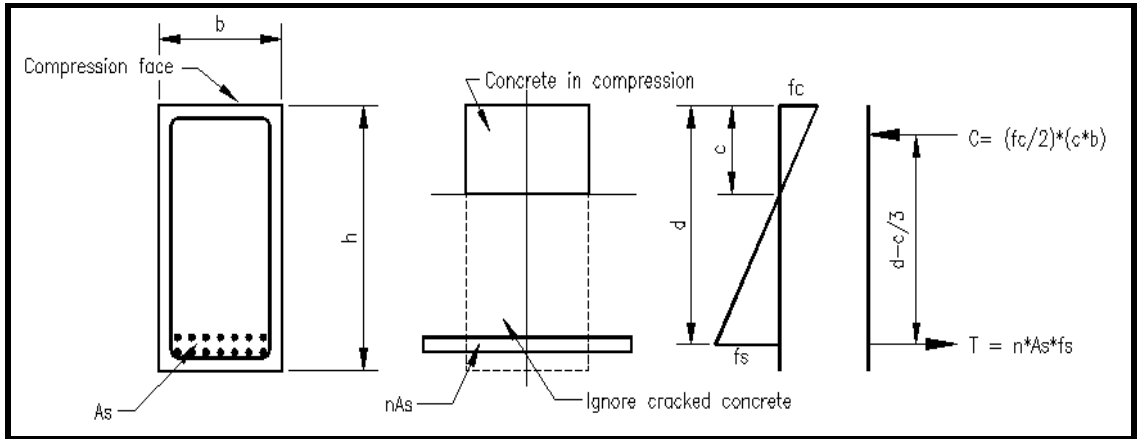


(a) Load-deflection diagram.



(b) Beam and loading.

In elastic service conditions, the stresses are indeed proportional to the strains. It's important to note that the linear stress distribution in the compression zone is a key consideration, as it varies from zero at the neutral axis to a maximum value at the compression face. Additionally, it's correct that the strain in the concrete is no longer equal to 0.003 when analysing under elastic service conditions.



## 6.0 ACI Code for Calculating Deflections:

**Table 24.2.2—Maximum permissible calculated deflections**

Member	Condition		Deflection to be considered	Deflection limitation
Flat roofs	Not supporting or attached to nonstructural elements likely to be damaged by large deflections Immediate deflection due to $L$		Immediate deflection due to maximum of $L$ , $S$ , and $R$	$l/180^{[1]}$
Floors			$l/360$	
Roof or floors	Supporting or attached to nonstructural elements	Likely to be damaged by large deflections	That part of the total deflection occurring after attachment of nonstructural elements, which is the sum of the time-dependent deflection due to all sustained loads and the immediate deflection due to any additional live load <sup>[2]</sup>	$l/480^{[3]}$
		Not likely to be damaged by large deflections		$l/240^{[4]}$

<sup>[1]</sup>Limit not intended to safeguard against ponding. Ponding shall be checked by calculations of deflection, including added deflections due to ponded water, and considering time-dependent effects of sustained loads, camber, construction tolerances, and reliability of provisions for drainage.

<sup>[2]</sup>Time-dependent deflection shall be calculated in accordance with 24.2.4, but shall be permitted to be reduced by amount of deflection calculated to occur before attachment of nonstructural elements. This amount shall be calculated on basis of accepted engineering data relating to time-deflection characteristics of members similar to those being considered.

<sup>[3]</sup>Limit shall be permitted to be exceeded if measures are taken to prevent damage to supported or attached elements.

<sup>[4]</sup>Limit shall not exceed tolerance provided for nonstructural elements.

#### 24.2.3 Calculation of immediate deflections

24.2.3.1 Immediate deflections shall be calculated using methods or formulas for elastic deflections, considering effects of cracking and reinforcement on member stiffness.

24.2.3.2 Effect of variation of cross-sectional properties, such as haunches, shall be considered when calculating deflections.

24.2.3.3 Deflections in two-way slab systems shall be calculated taking into account size and shape of the panel, conditions of support, and nature of restraints at the panel edges.

#### R24.2.3 Calculation of immediate deflections

R24.2.3.1 For calculation of immediate deflections of uncracked prismatic members, the usual methods or formulas for elastic deflections may be used with a constant value of  $E_c I_g$  along the length of the member. However, if the member is expected to crack at one or more sections, or if its depth varies along the span, a more rigorous calculation becomes necessary.

R24.2.3.3 The calculation of deflections for two-way slabs is challenging even if linear elastic behavior can be assumed. For immediate deflections, the values of  $E_c$  and  $I_g$  specified in 24.2.3.4 and 24.2.3.5, respectively, may be used (ACI 209R). However, other procedures and other values of the stiffness  $E_c I_g$  may be used if they result in predictions of deflection in reasonable agreement with the results of comprehensive tests.



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## CODE

24.2.3.4 Modulus of elasticity,  $E_c$ , shall be permitted to be calculated in accordance with 19.2.2.

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19.2.2.1 It shall be permitted to calculate  $E_c$  in accordance with (a) or (b):

(a) For values of  $w_c$  between 1440 and 2560 kg/m<sup>3</sup>

$$E_c = w_c^{1.5} 0.043 \sqrt{f'_c} \text{ (in MPa)} \quad (19.2.2.1.a)$$

(b) For normalweight concrete

$$E_c = 4700 \sqrt{f'_c} \text{ (in MPa)} \quad (19.2.2.1.b)$$

24.2.3.5 For nonprestressed members, unless obtained by a more comprehensive analysis, effective moment of inertia,  $I_e$ , shall be calculated in accordance with Table 24.2.3.5 using:

$$M_{cr} = \frac{f_r I_g}{y_t} \quad (24.2.3.5)$$

**Table 24.2.3.5—Effective moment of inertia,  $I_e$**

Service moment	Effective moment of inertia, $I_e$ , mm <sup>4</sup>	
$M_a \leq (2/3)M_{cr}$	$I_g$	(a)
$M_a > (2/3)M_{cr}$	$\frac{I_{cr}}{1 - \left( \frac{(2/3)M_{cr}}{M_a} \right)^2 \left( 1 - \frac{I_{cr}}{I_g} \right)}$	(b)

24.2.3.6 For continuous one-way slabs and beams,  $I_e$  shall be permitted to be taken as the average of values obtained from Table 24.2.3.5 for the critical positive and negative moment sections.

24.2.3.7 For prismatic one-way slabs and beams,  $I_e$  shall be permitted to be taken as the value obtained from Table 24.2.3.5 at midspan for simple and continuous spans, and at the support for cantilevers.

24.2.3.8 For prestressed Class U slabs and beams as defined in 24.5.2, it shall be permitted to calculate deflections based on  $I_g$ .

24.2.3.9 For prestressed Class T and Class C slabs and beams as defined in 24.5.2, deflection calculations shall be based on a cracked transformed section analysis. It shall be permitted to base deflection calculations on a bilinear moment-deflection relationship or  $I_e$  in accordance with Eq. (24.2.3.9a)

$$I_e = \left( \frac{M_{cr}}{M_a} \right)^3 I_g + \left[ 1 - \left( \frac{M_{cr}}{M_a} \right)^3 \right] I_{cr} \quad (24.2.3.9a)$$

where  $M_{cr}$  is calculated as

$$M_{cr} = \frac{(f_r + f_{pe}) I_g}{y_t} \quad (24.2.3.9b)$$

## 7.0 Factors Influences Immediate deflection:

Immediate deflections in beams and other structural elements are influenced by several key factors. These factors can be grouped into those related to the material properties, the geometry of the beam,

the type and magnitude of loads applied, and the boundary conditions. Here's a detailed look at these factors:

### Material Properties

#### 1. Young's Modulus (E):

- **Definition:** Young's modulus is a measure of the stiffness of a material.
- **Effect:** Higher values of Young's modulus result in less deflection for the same applied load because the material is stiffer.

#### 2. Material Density:

- **Definition:** Density affects the self-weight of the beam, which contributes to the overall load causing deflection.
- **Effect:** Heavier materials can increase the immediate deflection due to their own weight.

### Beam Geometry

#### 1. Moment of Inertia (I):

- **Definition:** Moment of inertia is a geometric property that reflects how mass is distributed relative to the neutral axis of the beam.
- **Effect:** A larger moment of inertia (which can be achieved by increasing the cross-sectional area or optimizing the shape) reduces deflection.

#### 2. Span Length (L):

- **Definition:** The distance between supports of a beam.
- **Effect:** Longer spans result in greater deflections. The deflection increases proportionally with the cube or fourth power of the span length, depending on the load type.

#### 3. Cross-Sectional Shape:

- **Definition:** The shape of the beam's cross-section (e.g., rectangular, I-beam, circular).
- **Effect:** Certain shapes provide better resistance to bending and deflection. For instance, I-beams are more efficient in resisting deflection compared to rectangular beams of the same material and cross-sectional area.

### Loading Conditions

#### 1. Type of Load:

- **Point Load:** A load applied at a single point.
- **Uniformly Distributed Load (UDL):** A load spread evenly across the length of the beam.
- **Effect:** Different load types create different deflection patterns. UDL typically causes more deflection compared to a point load for the same total load.

#### 2. Magnitude of Load:

- **Definition:** The amount of force or weight applied to the beam.

- **Effect:** Higher loads increase deflection proportionally.

### 3. Load Distribution:

- **Definition:** How the load is distributed along the beam.
- **Effect:** More concentrated loads cause higher local deflections compared to distributed loads.

## Boundary Conditions

### 1. Support Types:

- **Simply Supported:** The beam is supported at both ends but is free to rotate.
- **Fixed Support:** The beam is fixed at the ends, preventing rotation.
- **Cantilever:** The beam is fixed at one end and free at the other.
- **Effect:** Fixed supports reduce deflection compared to simply supported beams because they provide additional constraints. Cantilevers typically show the highest deflection for the same load and span length.

### 2. Number and Location of Supports:

- **Definition:** Additional supports can be placed along the span of the beam.
- **Effect:** Intermediate supports can significantly reduce the effective span and, consequently, the deflection.

## Other Influences

### 1. Temperature Effects:

- **Definition:** Changes in temperature can cause expansion or contraction of materials.
- **Effect:** Temperature variations can induce additional stresses and deflections, especially in materials with high coefficients of thermal expansion.

### 2. Initial Imperfections:

- **Definition:** Imperfections in the beam's geometry or material properties.
- **Effect:** These imperfections can lead to increased deflection under load due to stress concentrations and uneven load distribution.



## 7.0 Simplified Example:

A simply supported reinforced concrete beam with a span of 6 meters (20 feet) carries a uniformly distributed load of 10 kN/m (2000 lb/ft), including its own weight. The beam has a rectangular section with a width of 300 mm (12 inches) and a height of 600 mm (24 inches). The concrete compressive strength is  $f'_c = 30$  MPa (4000 psi), and the reinforcement ratio is sufficient to consider cracking.

### Step-by-Step Solution

1. Determine the Modulus of Elasticity ( $E_c$ ):

$$E_c = 4700\sqrt{30} = 25,748 \text{ MPa} = 25.75 \text{ GPa}$$

2. Calculate the Gross Moment of Inertia ( $I_g$ ):

$$I_g = \frac{bh^3}{12} = \frac{0.3 \times (0.6)^3}{12} = 0.0054 \text{ m}^4$$

**3. Determine the Cracking Moment ( $M_{cr}$ ):**

$$f_r = 7.5\sqrt{30} = 41 \text{ MPa}$$

$$S = \frac{bh^2}{6} = \frac{0.3 \times (0.6)^2}{6} = 0.018 \text{ m}^3$$

$$M_{cr} = f_r \cdot S = 41 \times 0.018 = 0.738 \text{ kNm}$$

**4. Calculate the Maximum Applied Moment ( $M_a$ ):**

For a simply supported beam with UDL,  $M_a = \frac{wL^2}{8}$ :

$$M_a = \frac{10 \times 6^2}{8} = 45 \text{ kNm}$$

**5. Calculate the Effective Moment of Inertia ( $I_e$ ):**

$$I_e = \frac{M_{cr}}{M_a} I_g + \left(1 - \frac{M_{cr}}{M_a}\right) I_{cr}$$

For simplicity, assume  $I_{cr} = \frac{I_g}{2}$  (this can vary based on the degree of cracking):

$$I_e = \frac{0.738}{45} \times 0.0054 + \left(1 - \frac{0.738}{45}\right) \times \frac{0.0054}{2}$$

$$I_e = 0.000088 \downarrow + 0.002616 = 0.002704 \text{ m}^4$$

**6. Calculate the Immediate Deflection ( $\delta_{max}$ ):**

$$\delta_{max} = \frac{5wL^4}{384E_cI_e}$$

$$\delta_{max} = \frac{5 \times 10 \times 6^4}{384 \times 25.75 \times 10^9 \times 0.002704}$$

$$\delta_{max} = \frac{5 \times 10 \times 1296}{384 \times 25.75 \times 10^9 \times 0.002704}$$

$$\delta_{max} = \frac{64,800}{266.62 \times 10^6}$$

$$\delta_{max} = 2.43 \times 10^{-4} \text{ m} = 0.243 \text{ mm}$$

This example provides a basic understanding of how to calculate deflection in a reinforced concrete beam using the double integration method. Real-world scenarios may involve more complex geometries and loading conditions, requiring more sophisticated analysis methods.

## 8.0 Summary

- Superposition is not applicable in computing deflections in RC members due to the presence of cracking in the member. This means that all deflection calculations must be done by stage, including all loads that occur simultaneously at each stage. Differential deformations can be found by taking the difference between stage results.
- Cracks form when the applied moment,  $M_a$ , exceeds the cracking moment,  $M_{cr}$
- The transformed section method is used to compute the relevant section properties. This is done by converting the steel to an equivalent area of concrete the computing the section properties of the transformed section.
- The location of the cracked section neutral axis is found by ignoring the concrete contribution in the tension zone, setting up the axial force equilibrium equation for remaining parts, then solving for the unknown neutral axis location.
- When applying the parallel axis theorem to the transformed steel areas, the  $I_o$  term can be ignored as being insignificant.
- An effective moment of inertia,  $I_e$ , is computed for use in the elastic deflection equations.  $I_e$  is a function of the applied load. The larger the applied load,  $M_a$ , the lower the value of  $I_e$  and the larger the deflections.
- Ultimately, the goal is to make the actual computed deflections to be less than the allowable deflections.

## 9.0 Conclusion

In conclusion, an understanding of deflection in structural concrete members is essential for ensuring the overall performance, serviceability, and safety of concrete structures. By considering deflection alongside other design considerations, engineers can develop robust and reliable designs that meet the functional and aesthetic requirements of the intended application.

This assignment sets the stage for delving deeper into the mechanics, analysis methods, and design considerations related to the deflection of structural concrete members.

Immediate deflections are influenced by a combination of material properties, beam geometry, loading conditions, and boundary conditions. Understanding these factors allows engineers to predict and control deflections to ensure that structures meet serviceability requirements and perform adequately throughout their service life.

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